

Function Inverses

State if the given functions are inverses.

1) $f(x) = x + 2$ $(f \circ g)(x) = \left(\frac{x-5}{8}\right) + 2 = \frac{x-5+16}{8} = \frac{x+11}{8}$ $g(x) = 3x$ $(f \circ g)(x) = \frac{1}{3}(3x) = x$
 $g(x) = \frac{x-5}{8}$ $(g \circ f)(x) = \frac{(x+2)-5}{8} = \frac{x-3}{8}$ $f(x) = \frac{1}{3}x$ $(g \circ f)(x) = 3\left(\frac{1}{3}x\right) = x$
 (No) (Yes)

* 3) $f(x) = -x^5 - 1$ $(f \circ g)(x) = -(\sqrt[5]{x} + 1)^5 - 1$ $h(x) = \sqrt[3]{-x+1}$ $(h \circ f)(x) = \sqrt[3]{-(x^3+1)+1} = \sqrt[3]{-x^3-x^3+1+1} = \sqrt[3]{-2x^3+2} = \sqrt[3]{-2(x^3-1)} = \sqrt[3]{-2(x-1)(x^2+x+1)}$
 $g(x) = \sqrt[5]{x} + 1$ $(g \circ f)(x) = \sqrt[5]{-x^5-1} + 1$ $f(n) = -n^5 - 1$ $h(n) = \sqrt[3]{-n+1}$ $(f \circ h)(x) = -(\sqrt[3]{-x+1})^3 + 1 = -(-x+1) + 1 = x - 1 + 1 = x$
 (No) (Yes)

5) $f(n) = \frac{4}{-n+3}$ $g(x) = \frac{-4}{x} + 3$ $(f \circ g)(x) = \frac{4}{-\left(\frac{-4}{x} + 3\right) + 3} = \frac{4}{\frac{4}{x} - 3 + 3} = \frac{4}{\frac{4}{x}} = 4 \cdot \frac{x}{4} = x$ (Yes)
 6) $h(x) = \frac{2}{x-1} - 2$ $(h \circ f)(x) = \frac{2}{\left(\frac{-4}{x+1} + 3\right) - 1} - 2 = \frac{2}{\frac{-4}{x+1} + 2} - 2 = \frac{2}{\frac{-4 + 2(x+1)}{x+1}} - 2 = \frac{2}{\frac{-4 + 2x + 2}{x+1}} - 2 = \frac{2}{\frac{2x-2}{x+1}} - 2 = \frac{2 \cdot (x+1)}{2(x-1)} - 2 = \frac{x+1}{x-1} - 2 = \frac{x+1-2(x-1)}{x-1} = \frac{x+1-2x+2}{x-1} = \frac{-x+3}{x-1}$ (No)

Find the inverse of each function.

7) $g(x) = \frac{-x-4}{4}$ $x = \frac{-y-4}{4}$
 $4x = -y-4$
 $4x+4 = -y$
 $g^{-1}(x) = -4x-4$

8) $g(x) = -2x-4$ $x = -2y-4$
 $x+4 = -2y$
 $g^{-1}(x) = -\frac{1}{2}x-2$

9) $g(x) = \sqrt[5]{x}$ $x = \sqrt[5]{y}$
 $y = x^5$
 $g^{-1}(x) = x^5$

10) $g(x) = \frac{4 + \sqrt[3]{4x}}{2}$ $4y = (2x-4)^3$
 $y = \frac{(2x-4)^3}{4}$
 $g^{-1}(x) = \frac{(2x-4)^3}{4}$

As soon as I see this isn't x, no

$$11) g(x) = \frac{3}{x-1} + 2$$

$$x = \frac{3}{y-1} + 2$$

$$\frac{x-2}{1} = \frac{3}{y-1}$$

$$(y-1)(x-2) = 3$$

$$y-1 = \frac{3}{x-2}$$

$$g^{-1}(x) = \frac{3}{x-2} + 1$$

$$12) f(x) = \frac{1}{x-1} - 2$$

$$x = \frac{1}{y-1} - 2$$

$$x+2 = \frac{1}{y-1}$$

$$(y-1)(x+2) = 1$$

$$y-1 = \frac{1}{x+2}$$

$$f^{-1}(x) = \frac{1}{x+2} + 1$$

$$13) g(x) = 2(x-3)^3$$

$$x = 2(y-3)^3$$

$$\frac{x}{2} = (y-3)^3$$

$$\sqrt[3]{\frac{x}{2}} = y-3$$

$$\frac{\sqrt[3]{x}}{\sqrt[3]{2}} + 3 = y$$

$$\frac{\sqrt[3]{4x}}{2} + 3 = y$$

$$g^{-1}(x) = \frac{\sqrt[3]{4x+6}}{2} \text{ or } \frac{\sqrt[3]{4x}}{2} + 3$$

$$14) h(x) = \frac{-5x+15}{7}$$

$$x = \frac{-5y+15}{7}$$

$$7x = -5y+15$$

$$7x-15 = -5y$$

$$h^{-1}(x) = \frac{-7}{5}x + 3$$

$$15) h(n) = \sqrt[3]{n+1} - 2$$

$$x = \sqrt[3]{y+1} - 2$$

$$x+2 = \sqrt[3]{y+1}$$

$$(x+2)^3 = y+1$$

$$h^{-1}(n) = (n+2)^3 - 1$$

$$16) f(x) = \sqrt[3]{x+3}$$

$$x = \sqrt[3]{y+3}$$

$$x^3 = y+3$$

$$f^{-1}(x) = x^3 - 3$$

$$17) g(x) = 2x^3 - 2$$

$$x = \sqrt[3]{\frac{y+2}{2}}$$

$$x+2 = 2y^3$$

$$\frac{x+2}{2} = y^3$$

$$g^{-1}(x) = \sqrt[3]{\frac{x+2}{2}}$$

$$18) h(x) = 2(x-2)^5$$

$$\frac{x}{2} = (y-2)^5$$

$$\sqrt[5]{\frac{x}{2}} = y-2$$

$$\sqrt[5]{\frac{x}{2}} = y-2$$

$$h^{-1}(x) = \sqrt[5]{\frac{x}{2}} + 2$$

$$19) f(n) = -2(n+3)^3$$

$$\frac{x}{-2} = (y+3)^3$$

$$\sqrt[3]{\frac{x}{-2}} = y+3$$

$$\sqrt[3]{\frac{x}{-2}} = y+3$$

$$f^{-1}(n) = \sqrt[3]{\frac{n}{-2}} - 3$$

$$20) f(x) = \frac{4}{x+2}$$

$$x = \frac{4}{y+2}$$

$$(y+2)x = 4$$

$$y+2 = \frac{4}{x}$$

$$f^{-1}(x) = \frac{4}{x} - 2$$

$$21) f(x) = \sqrt[3]{-\frac{x}{2}}$$

$$x = \sqrt[3]{-\frac{y}{2}}$$

$$x^3 = \frac{-y}{2}$$

$$2x^3 = -y$$

$$f^{-1}(x) = -2x^3$$

$$22) f(x) = -7x - 4$$

$$x = -7y - 4$$

$$x + 4 = -7y$$

$$f^{-1}(x) = \frac{-x}{7} - \frac{4}{7}$$

$$23) f(n) = \sqrt[5]{n-1} - 2$$

$$x = \sqrt[5]{y-1} - 2$$

$$x + 2 = \sqrt[5]{y-1}$$

$$(x+2)^5 = y-1$$

$$f^{-1}(n) = (n+2)^5 + 1$$

$$24) g(x) = (x-2)^3 - 2$$

$$x = (y-2)^3 - 2$$

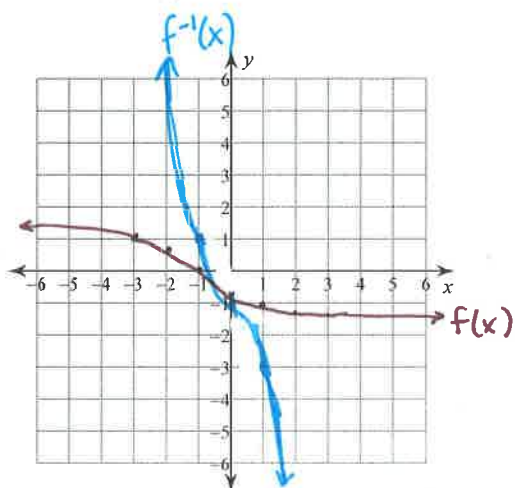
$$x + 2 = (y-2)^3$$

$$\sqrt[3]{x+2} = y-2$$

$$y = \sqrt[3]{x+2} + 2$$

Find the inverse of each function. Then graph the function and its inverse.

$$25) f(x) = \sqrt[3]{\frac{-x-1}{2}}$$



$$x = \sqrt[3]{\frac{-y-1}{2}}$$

$$x^3 = \frac{-y-1}{2}$$

$$2x^3 = -y-1$$

$$2x^3 + 1 = -y$$

$$f^{-1}(x) = -2x^3 - 1$$

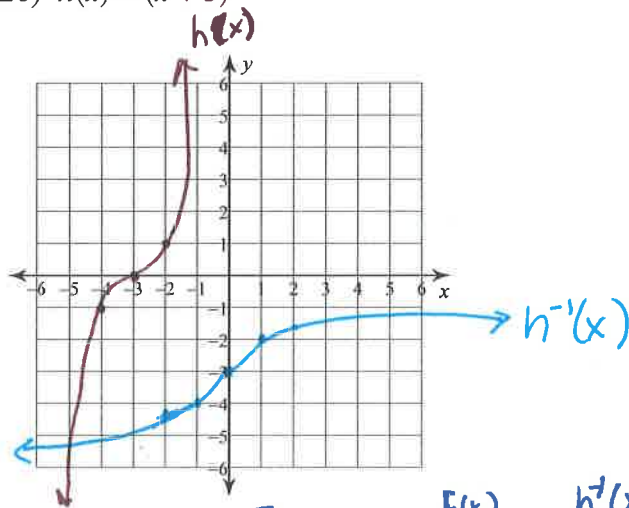
x	y
-3	1
-2	.7937
-1	0
0	-7.937
1	-1
2	-1.145
3	-1.26

f(x)

x	y
-3	53
-2	15
-1	1
0	-1
1	-3
2	-17
3	-55

f⁻¹(x)

$$26) h(x) = (x+3)^5$$



$$x = (y+3)^5$$

$$\sqrt[5]{x} = y+3$$

$$h^{-1}(x) = \sqrt[5]{x} - 3$$

f(x)		h ⁻¹ (x)	
x	y	x	y
-5	-32	-2	-4.149
-4	-1	-1	-4
-3	0	0	-3
-2	1	1	-2
-1	32	2	-1.857

Function Inverses

State if the given functions are inverses.

$$1) \begin{aligned} f(x) &= x + 2 \\ g(x) &= \frac{x - 5}{8} \end{aligned}$$

$$2) \begin{aligned} g(x) &= 3x \\ f(x) &= \frac{1}{3}x \end{aligned}$$

$$3) \begin{aligned} f(x) &= -x^5 - 1 \\ g(x) &= \sqrt[5]{x} + 1 \end{aligned}$$

$$4) \begin{aligned} h(x) &= \sqrt[3]{-x + 1} \\ f(x) &= -x^3 + 1 \end{aligned}$$

$$5) \begin{aligned} f(x) &= \frac{4}{-x + 3} \\ g(x) &= -\frac{4}{x} + 3 \end{aligned}$$

$$6) \begin{aligned} h(x) &= \frac{2}{x - 1} - 2 \\ f(x) &= -\frac{4}{x + 1} + 3 \end{aligned}$$

Find the inverse of each function.

$$7) g(x) = \frac{-x - 4}{4}$$

$$8) g(x) = -2x - 4$$

$$9) g(x) = \sqrt[5]{x}$$

$$10) g(x) = \frac{4 + \sqrt[3]{4x}}{2}$$

$$11) g(x) = \frac{3}{x-1} + 2$$

$$12) f(x) = \frac{1}{x-1} - 2$$

$$13) g(x) = 2(x-3)^3$$

$$14) h(x) = \frac{-5x+15}{7}$$

$$15) h(n) = \sqrt[3]{n+1} - 2$$

$$16) f(x) = \sqrt[3]{x+3}$$

$$17) g(x) = 2x^3 - 2$$

$$18) h(x) = 2(x-2)^5$$

$$19) f(n) = -2(n+3)^3$$

$$20) f(x) = \frac{4}{x+2}$$

$$21) f(x) = \sqrt[3]{-\frac{x}{2}}$$

$$22) f(x) = -7x - 4$$

$$23) f(n) = \sqrt[5]{n-1} - 2$$

$$24) g(x) = (x-2)^3 - 2$$

Find the inverse of each function. Then graph the function and its inverse.

$$25) f(x) = \sqrt[3]{\frac{-x-1}{2}}$$

$$26) h(x) = (x+3)^5$$

