

Rational Expressions Part 1

State the excluded values for each.

1) $\frac{36r}{40r^2}$ $\frac{9}{10r}$
 $\boxed{\{0\}}$

2) $\frac{42n^2}{12n+48} = \frac{7n^2}{2(n+4)}$
 $\boxed{\{-4\}}$

3) $\frac{2r-2}{6r^2-25r-25}$ $\frac{2(r-1)}{(r-5)(6r+5)}$
 $6r^2+5r-30r-25$
 $r(6r+5)-5(6r+5)$
 $\boxed{\{5, -5/6\}}$

4) $\frac{2r^2-8r+8}{3r^3-8r^2+4r}$ $\boxed{\{0, 2, 2/3\}}$
 $r(3r^2-8r+4)$
 $r(3r^2-6r-2r+4)$
 $r(3r(r-2)-2(r-2))$
 $r(r-2)(3r-2)$

Simplify each expression.

5) $\frac{12b}{16b}$ $\boxed{\frac{3}{4}}$ $b \neq 0$

6) $\frac{36b^2}{36b^3}$ $\boxed{\frac{1}{b}}$ $b \neq 0$

7) $\frac{25}{35r-20}$ $\frac{25}{5(7r-4)} = \boxed{\frac{5}{7r-4}}$
 $r \neq 4/7$

8) $\frac{x^2-8x+7}{x-7}$ $\frac{(x-7)(x-1)}{(x-7)} = \boxed{x-1}$
 $x \neq 7$

9) $\frac{16k+72}{24k+56}$ $\frac{8(2k+9)}{8(3k+7)} = \boxed{\frac{2k+9}{3k+7}}$
 $k \neq -7/3$

10) $\frac{9x-18}{x^2-7x+10}$ $\frac{9(x-2)}{(x-5)(x-2)} = \boxed{\frac{9}{x-5}}$
 $x \neq 5$
 $x \neq 2$

$$\frac{-60}{-15} \quad \frac{105}{-15-7}$$

$$11) \frac{15b^3 - 33b^2 - 36b}{5b^2 - 22b + 21}$$

$$\frac{3b(5b^2 - 11b - 12)}{5b^2 - 22b + 21} = \frac{3b(5b^2 - 15b + 4b - 12)}{5b^2 - 15b - 7b + 21}$$

$$= \frac{3b[5b(b-3) + 4(b-3)]}{5b(b-3) - 7(b-3)} = \frac{3b(b-3)(5b+4)}{(b-3)(5b-7)}$$

$$= \boxed{\frac{3b(5b+4)}{5b-7}} \quad \begin{array}{l} b \neq 3 \\ b \neq \frac{7}{5} \end{array}$$

$$12) \frac{2n^2 - 18n + 16}{15n^3 - 135n^2 + 120n}$$

$$\frac{2(n^2 - 9n + 8)}{15n(n^2 - 9n + 8)} = \frac{2(\cancel{n-8})(n-1)}{15n(\cancel{n-8})(n-1)}$$

$$\boxed{\frac{2}{15n}}$$

$$\begin{array}{l} n \neq 8 \\ n \neq 1 \end{array}$$

$$13) \frac{12n^2 - 12}{20n + 20}$$

$$\frac{12(n^2 - 1)}{20(n+1)} = \frac{12(n-1)(\cancel{n+1})}{20(n+1)}$$

$$\boxed{\frac{3(n-1)}{5}}$$

$$n \neq -1$$

$$14) \frac{4x^2 + 6x + 2}{3x + 21} = \frac{2(2x^2 + 3x + 1)}{3(x+7)}$$

$$= \frac{2(2x^2 + 2x + x + 1)}{3(x+7)} = \frac{2[2x(x+1) + 1(x+1)]}{3(x+7)}$$

$$= \boxed{\frac{2(x+1)(2x+1)}{3(x+7)}}$$

$$x \neq -7$$

$$15) \frac{14v^3 - 38v^2 - 12v}{3v^2 - 16v + 21}$$

$$\frac{-42}{-21+2} \quad \frac{63}{-9-7}$$

$$\frac{2(7v^3 - 19v^2 - 6v)}{3v^2 - 16v + 21} = \frac{2v(7v^2 - 21v + 2v - 6)}{(3v^2 - 9v - 7v + 21)}$$

$$\frac{2v[7v(v-3) + 2(v-3)]}{3v(v-3) - 7(v-3)} = \frac{2v(v-3)(7v+2)}{(v-3)(3v-7)}$$

$$\boxed{\frac{2v(7v+2)}{3v-7}} \quad \begin{array}{l} v \neq 3 \\ v \neq \frac{7}{3} \end{array}$$

$$16) \frac{2n^2 - 11n + 9}{21n^3 - 48n^2 + 27n}$$

$$\frac{18}{-9-2} \quad \frac{63}{-9-7}$$

$$\frac{2n^2 - 9n - 2n + 9}{3n(7n^2 - 16n + 9)} = \frac{n(2n-9) - 1(2n-9)}{3n[7n^2 - 9n - 7n + 9]}$$

$$\frac{(n-1)(2n-9)}{3n[(7n-9) - 1(7n-9)]} = \frac{(n-1)(2n-9)}{3n(\cancel{7n-9})(7n-9)}$$

$$\boxed{\frac{2n-9}{3n(7n-9)}}$$

$$\begin{array}{l} n \neq 0 \\ n \neq \frac{9}{7} \\ n \neq 1 \end{array}$$

Rational Expressions Part 1

State the excluded values for each.

1) $\frac{36r}{40r^2}$

2) $\frac{42n^2}{12n + 48}$

3) $\frac{2r - 2}{6r^2 - 25r - 25}$

4) $\frac{2r^2 - 8r + 8}{3r^3 - 8r^2 + 4r}$

Simplify each expression.

5) $\frac{12b}{16b}$

6) $\frac{36b^2}{36b^3}$

7) $\frac{25}{35r - 20}$

8) $\frac{x^2 - 8x + 7}{x - 7}$

9) $\frac{16k + 72}{24k + 56}$

10) $\frac{9x - 18}{x^2 - 7x + 10}$

$$11) \frac{15b^3 - 33b^2 - 36b}{5b^2 - 22b + 21}$$

$$12) \frac{2n^2 - 18n + 16}{15n^3 - 135n^2 + 120n}$$

$$13) \frac{12n^2 - 12}{20n + 20}$$

$$14) \frac{4x^2 + 6x + 2}{3x + 21}$$

$$15) \frac{7v^3 - 67v^2 + 36v}{8v^2 + 56v}$$

$$16) \frac{2n^2 - 11n + 9}{21n^3 - 48n^2 + 27n}$$