

Ellipses & ~~Hyperbolas~~

Identify the center, vertices, and foci of each. Then sketch the graph.

1) $\frac{x^2}{49} + (y+2)^2 = 1$ *major*

Center (0, -2)
a=7 b=1

major vertices (-7, -2)(7, -2)

minor vertices: (0, -1)(0, -3)

foci: $(-4\sqrt{3}, -2)(4\sqrt{3}, -2)$

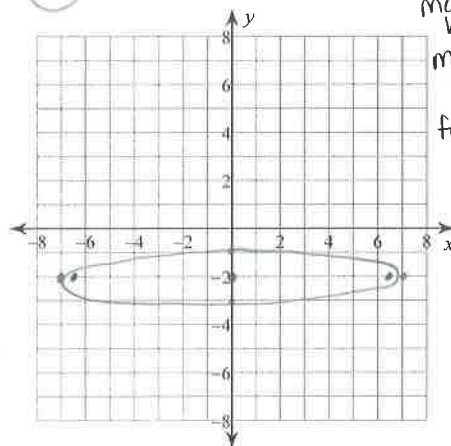
$a^2 - c^2 = b^2$

$7^2 - c^2 = 1^2$

$49 - c^2 = 1$

$48 = c^2$

$c = 4\sqrt{3}$



2) $\frac{(x-3)^2}{16} + (y-5)^2 = 1$ *major*

Center (3, 5)
a=4 b=1

major vertices: (-1, 5)(7, 5)

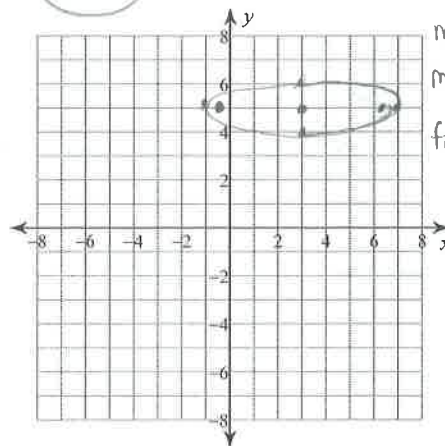
minor vertices: (3, 4)(3, 6)

foci: $(3-\sqrt{15}, 5)(3+\sqrt{15}, 5)$

$16 - c^2 = 1$

$c^2 = 15$

$c = \sqrt{15}$



3) $\frac{(x-1)^2}{9} + \frac{(y-4)^2}{4} = 1$ *major*

Center (1, 4)
a=3 b=2

major: (-2, 4)(4, 4)

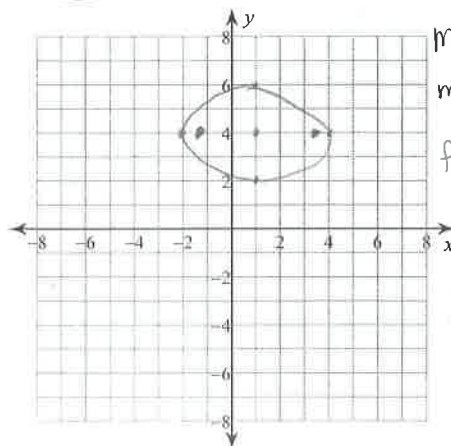
minor: (1, 2)(1, 6)

foci: $(1-\sqrt{5}, 4)(1+\sqrt{5}, 4)$

$9 - c^2 = 4$

$c^2 = 5$

$c = \sqrt{5}$



4) $\frac{(x+1)^2}{15} + \frac{y^2}{35} = 1$ *major*

Center (-1, 0)
a= $\sqrt{35}$ b= $\sqrt{15}$

major (-1, $\sqrt{35}$)(-1, $-\sqrt{35}$)

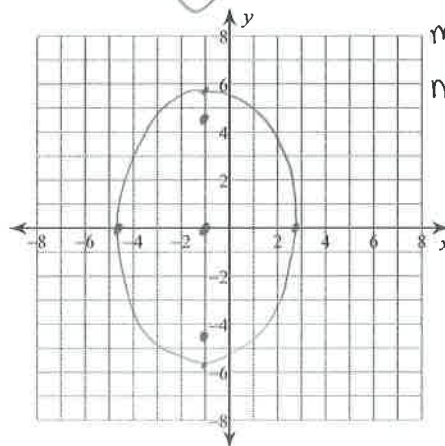
minor (-1, $\sqrt{15}$, 0)(-1, $-\sqrt{15}$, 0)

foci: $(-1, 2\sqrt{5})(-1, -2\sqrt{5})$

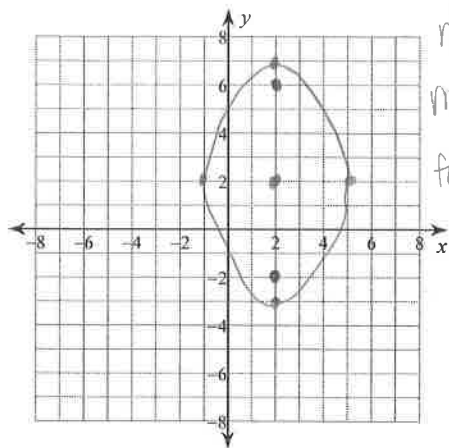
$35 - c^2 = 15$

$c^2 = 20$

$c = 2\sqrt{5}$

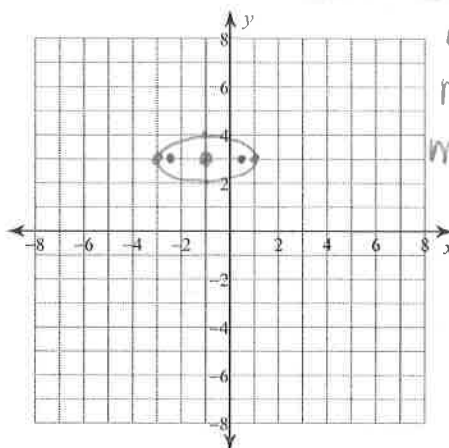


$$5) \frac{(x-2)^2}{9} + \frac{(y-2)^2}{25} = 1$$



Center (2, 2)
 $a=5$ $b=3$
 major: (2, 7)(2, -3)
 minor: (-1, 2)(5, 2)
 foci: (2, 6)(2, -2)
 $25 - c^2 = 9$
 $c^2 = 16$
 $c = 4$

$$6) \frac{(x+1)^2}{4} + (y-3)^2 = 1$$



center (-1, 3)
 $a=2$ $b=1$
 major: (-3, 3)(1, 3)
 minor: (-1, 4)(-1, 2)
 foci: $(-1-\sqrt{3}, 3)$ $(-1+\sqrt{3}, 3)$
 $4 - c^2 = 1$
 $c^2 = 3$
 $c = \sqrt{3}$

Use the information provided to write the standard form equation of each ellipse.

$$7) 9x^2 + 16y^2 + 162x - 192y + 9 = 0$$

$$9(x^2 + 18x + 81 - 81) + 16(y^2 - 12y + 36 - 36) + 9 = 0$$

$$9(x+9)^2 - 729 + 16(y-6)^2 - 576 + 9 = 0$$

$$9(x+9)^2 + 16(y-6)^2 = 1296$$

$$\frac{(x+9)^2}{144} + \frac{(y-6)^2}{81} = 1$$

$$9) 5x^2 + y^2 + 90x - 6y + 214 = 0$$

$$5(x^2 + 18x + 81 - 81) + (y^2 - 6y + 9 - 9) + 214 = 0$$

$$5(x+9)^2 - 405 + (y-3)^2 - 9 + 214 = 0$$

$$5(x+9)^2 + (y-3)^2 = 200$$

$$\frac{(x+9)^2}{40} + \frac{(y-3)^2}{200} = 1$$

11) Vertices: (0, -5), (0, -15)
 Foci: (0, -6), (0, -14)
 $(\frac{0+0}{2}, \frac{-6+(-14)}{2})$ $b^2 = 5^2 - 4^2$
 $b^2 = 25 - 16$
 $b^2 = 9$
 center (0, -10) $b = 3$
 $c = 4$ $a = 5$

$$\frac{x^2}{9} + \frac{(y+10)^2}{25} = 1$$

major = y

13) Vertices: (6, -4), (-8, -4)
 Foci: $(-1 + \sqrt{13}, -4)$, $(-1 - \sqrt{13}, -4)$
 $(\frac{6+(-8)}{2}, \frac{-4+(-4)}{2})$ $b^2 = 49 - 13$
 $b^2 = 36$
 $b = 6$
 center (-1, -4)
 $c = \sqrt{13}$ $a = 7$

$$\frac{(x+1)^2}{49} + \frac{(y+4)^2}{36} = 1$$

major = x

$$8) 16x^2 + 9y^2 + 224x - 108y - 188 = 0$$

$$16(x^2 + 14x + 49 - 49) + 9(y^2 - 12y + 36 - 36) - 188 = 0$$

$$16(x+7)^2 - 784 + 9(y-6)^2 - 324 - 188 = 0$$

$$16(x+7)^2 + 9(y-6)^2 = 1296$$

$$\frac{(x+7)^2}{81} + \frac{(y-6)^2}{144} = 1$$

$$10) x^2 + 3y^2 + 14x - 54y + 277 = 0$$

$$x^2 + 14x + 49 - 49 + 3(y^2 - 18y + 81 - 81) + 277 = 0$$

$$(x+7)^2 - 49 + 3(y-9)^2 - 243 + 277 = 0$$

$$(x+7)^2 + 3(y-9)^2 = 15$$

$$\frac{(x+7)^2}{15} + \frac{(y-9)^2}{5} = 1$$

12) Vertices: (0, 16), (0, -10)
 Foci: (0, 15), (0, -9)
 $(\frac{0+0}{2}, \frac{16+(-10)}{2})$ $b^2 = 169 - 144$
 $b^2 = 25$
 $b = 5$
 center (0, 3)
 $c = 12$ $a = 13$

$$\frac{x^2}{25} + \frac{(y-3)^2}{169} = 1$$

major = y

14) Vertices: (6, 4), (6, -20)
 Foci: $(6, -8 + 2\sqrt{11})$, $(6, -8 - 2\sqrt{11})$
 $(\frac{6+6}{2}, \frac{4+(-20)}{2})$ $b^2 = 144 - 44$
 $b^2 = 100$
 $b = 10$
 center (6, -8)
 $c = 2\sqrt{11}$ $a = 12$

$$\frac{(x-6)^2}{100} + \frac{(y+8)^2}{144} = 1$$

major = y