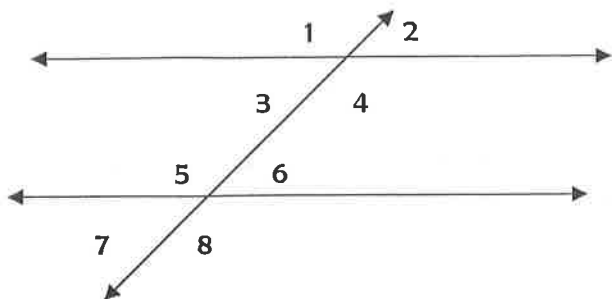


## Unit 3 Review

1. Identify types of angles

< 1 and < 4: Vertical angles< 5 and < 3: same-side interior< 2 and < 6: corresponding< 1 and < 8: alternate exterior< 3 and < 6: alternate interiorc

2. A regular polygon has

- equal sides
- equal angles
- both equal angles and equal sides
- parallel sides

c

3. A scalene triangle has

- three equal sides
- two or more equal sides
- no equal sides
- two right angles

b

4. An equiangular polygon has

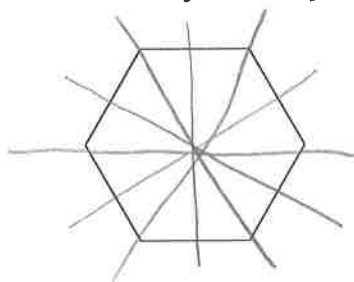
- equal sides
- equal angles
- both equal angles and equal sides
- parallel sides

b

5. An isosceles triangle has

- three equal sides
- two or more equal sides
- no equal sides
- two right angles

6. Sketch every axis of symmetry. Note the number of axes.



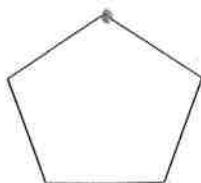
Number of axes:

6

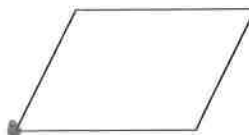
Number of axes:

1

7. Determine the order for each figure's rotational symmetry.



Order :

5

Order:

2

Formulas for Sum of Interior Angles, Each Angle, Sum of Exterior Angles

Sum of interior = $(n-2)180^\circ$	Each interior = $\frac{(n-2)180}{n}$	Sum of exterior = 360	Each exterior = $\frac{360}{n}$
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8. What is the sum of the exterior angles of an 11-gon?

$$360^\circ$$

9. How many <sup>n</sup>sides would a regular polygon have if the sum of the interior angles is 10,620 degrees?

$$S_i = (n-2)180$$

$$\frac{10620}{180} = \frac{(n-2)180}{180}$$

$$59 = n - 2$$

$$\begin{array}{r} + 2 \\ \hline 61 = n \end{array}$$

10. What is the sum of the interior angles of a 19-gon?

$$(19-2)180$$

$$17 \cdot 180$$

$$3060^\circ$$

11. How many <sup>n</sup>sides would a regular polygon have if each exterior angle is 7.5 degrees?

$$E_e = \frac{360}{n}$$

$$\frac{7.5}{1} = \frac{360}{n}$$

$$\frac{7.5n}{7.5} = \frac{360}{7.5}$$

$$n = 48$$

12. What is the measure of each interior angle of a regular dodecagon?

$$\frac{(12-2)180}{12} = \frac{10(180)}{12} = \frac{1800}{12}$$

$$150^\circ$$

13. What is the exterior angle at an interior angle of 110 degrees?

$$\frac{180}{1} - 110$$

$$70$$

14. What is the measure of each exterior angle of a regular 27-gon?

$$\frac{360}{27} = 13.3^\circ$$

15. How many <sup>n</sup>sides would a regular polygon have if each interior angle is 160 degrees?

$$E_i = \frac{(n-2)180}{n}$$

$$\frac{160}{1} = \frac{(n-2)180}{n}$$

$$160n = 180(n-2)$$

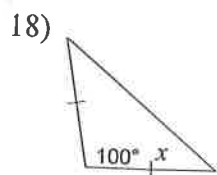
$$160n = 180n - 360$$

$$\begin{array}{r} -180n \\ \hline -20n = -360 \end{array}$$

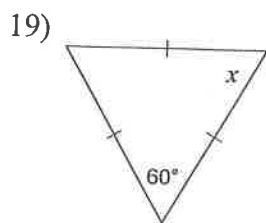
$$\frac{-20n}{-20} = \frac{-360}{-20}$$

$$n = 18$$

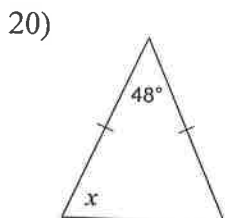
Find the value of  $x$ .



$$\begin{array}{r} 180 \\ -100 \\ \hline 80 \end{array} \quad 80/2 = \boxed{40}$$

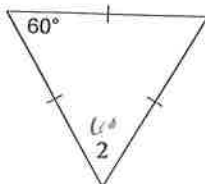


$$x = \boxed{60}$$



$$\begin{array}{r} 180 \\ -48 \\ \hline 132/2 = \end{array} \boxed{66}$$

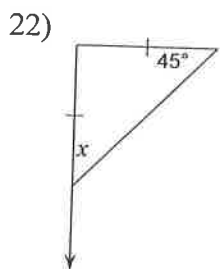
21)  $m\angle 2 = 9x + 6$



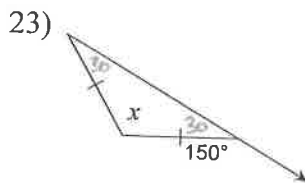
$$\begin{array}{r} 60 = 9x + 6 \\ -6 \quad -6 \\ \hline \end{array}$$

$$\frac{54}{9} = \frac{9x}{9}$$

$$x = \boxed{6}$$

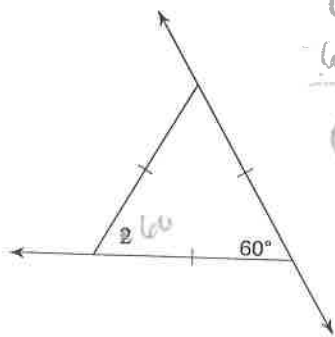


$$x = \boxed{45}$$



$$\begin{array}{r} 30 \quad 180 \\ +30 \quad -60 \\ \hline 60 \quad x = \end{array} \boxed{120}$$

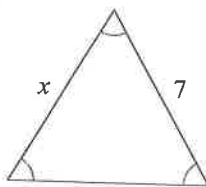
24)  $m\angle 2 = x + 68$



$$\begin{array}{r} 60 = x + 68 \\ -68 \quad -68 \\ \hline \end{array}$$

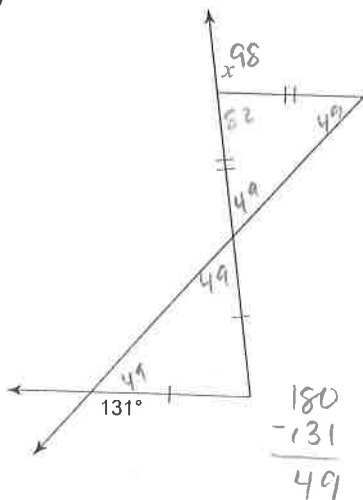
$$\boxed{-8 = x}$$

25)



$$\boxed{x = 7}$$

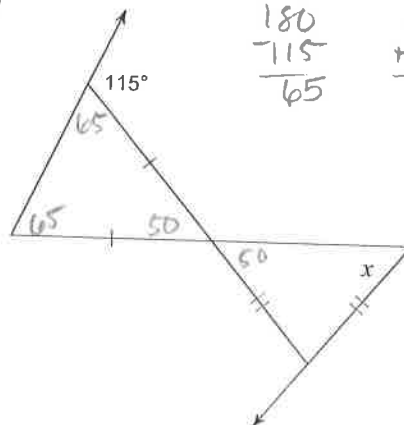
26)



$$\begin{array}{r} 49 \quad 180 \\ +49 \quad -98 \\ \hline 98 \quad \quad 82 \end{array}$$

$$\boxed{x = 98}$$

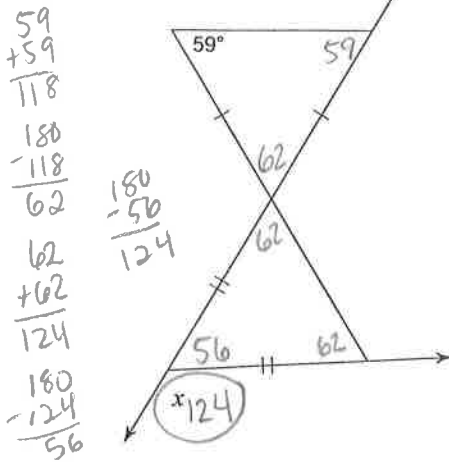
27)



$$\begin{array}{r} 180 \\ -115 \\ \hline 65 \end{array} \quad \begin{array}{r} 65 \\ +65 \\ \hline 130 \end{array} \quad \begin{array}{r} 180 \\ -130 \\ \hline 50 \end{array}$$

$$\boxed{x = 50}$$

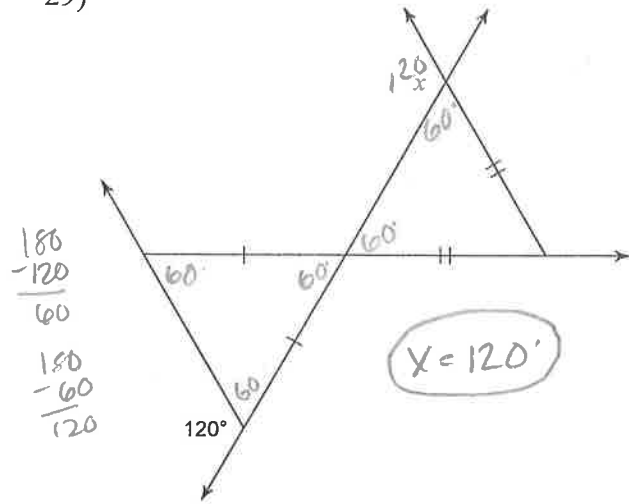
28)



$x = 124^\circ$

$$\begin{array}{r} 59 \\ + 59 \\ \hline 118 \\ 180 \\ - 118 \\ \hline 62 \\ 62 \\ + 62 \\ \hline 124 \\ 180 \\ - 124 \\ \hline 56 \end{array}$$

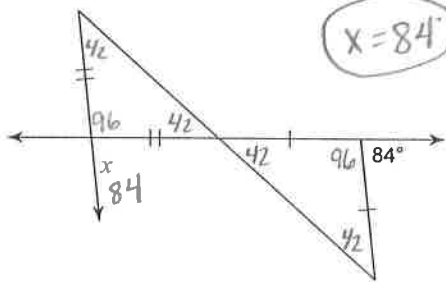
29)



$x = 120^\circ$

$$\begin{array}{r} 180 \\ - 120 \\ \hline 60 \\ 180 \\ - 60 \\ \hline 120 \end{array}$$

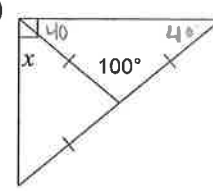
30)



$x = 84^\circ$

$$\begin{array}{r} 180 \\ - 84 \\ \hline 96 \\ 180 \\ - 96 \\ \hline 84/2 = 42 \end{array}$$

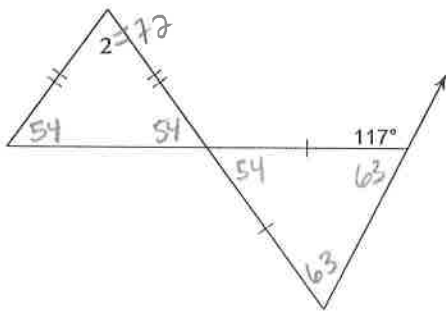
31)



$x = 50$

$$\begin{array}{r} 180 \\ - 100 \\ \hline 80/2 = 40 \\ 90 \\ - 40 \\ \hline 50 \end{array}$$

32)  $m\angle 2 = x + 78$

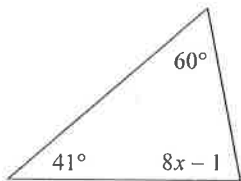


$$\begin{array}{r} 180 \\ - 117 \\ \hline 63 \\ 63 \\ + 63 \\ \hline 126 \\ 180 \\ - 126 \\ \hline 54 \\ 54 \\ + 54 \\ \hline 108 \\ 180 \\ - 108 \\ \hline 72 \end{array}$$

$$\begin{array}{r} 72 = x + 78 \\ - 78 \\ \hline -6 = x \end{array}$$

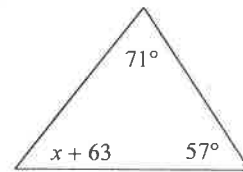
Solve for x.

33)



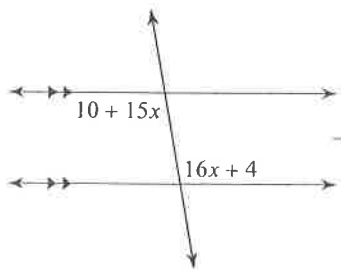
$$\begin{array}{r} 41 + 60 + 8x - 1 = 180 \\ 8x + 100 = 180 \\ - 100 \quad - 100 \\ \hline 8x = 80 \\ \frac{8x}{8} = \frac{80}{8} \\ \hline x = 10 \end{array}$$

34)



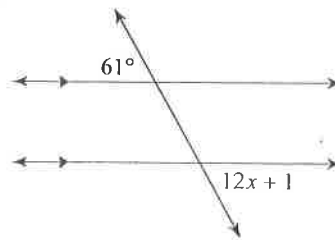
$$\begin{array}{r} 71 + 57 + x + 63 = 180 \\ x + 191 = 180 \\ - 191 \quad - 191 \\ \hline x = -11 \end{array}$$

35)



$$\begin{array}{r} 10 + 15x = 16x + 4 \\ - 15x \quad - 15x \\ \hline 10 = x + 4 \\ - 4 \quad - 4 \\ \hline 6 = x \end{array}$$

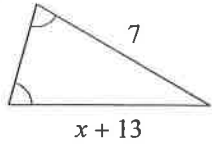
36)



$$\begin{array}{r} 61 = 12x + 1 \\ - 1 \quad - 1 \\ \hline 60 = 12x \\ \frac{60}{12} = \frac{12x}{12} \\ \hline 5 = x \end{array}$$

Find the value of  $x$ .

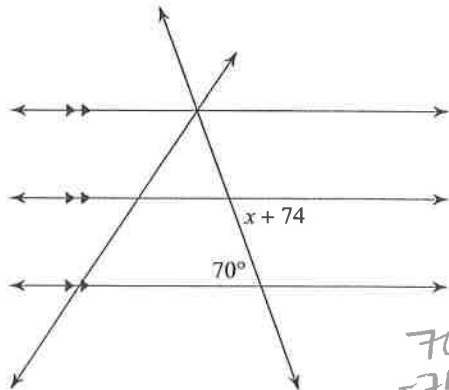
37)



$$\begin{array}{r} 7 = x + 13 \\ -13 \quad -13 \\ \hline -6 = x \end{array}$$

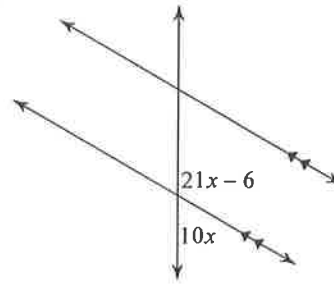
Solve for  $x$ .

38)



$$\begin{array}{r} 70 = x + 74 \\ -74 \quad -74 \\ \hline -4 = x \end{array}$$

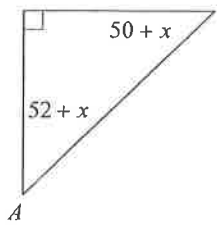
39)



$$\begin{array}{r} 21x - 6 + 10x = 180 \\ 31x - 6 = 180 \\ +6 \quad +6 \\ \hline 31x = 186 \\ \hline 31 \quad 31 \\ \hline x = 6 \end{array}$$

Find the measure of angle A.

40)

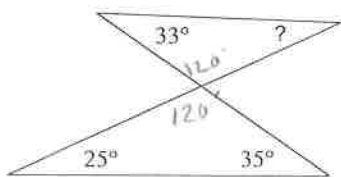


$$\begin{array}{r} 90 + 50 + x + 52 + x = 180 \\ 192 + 2x = 180 \\ -192 \quad -192 \\ \hline 2x = -12 \\ \hline x = -6 \end{array}$$

$$\begin{array}{r} m\angle A = 52 + x \\ = 52 + (-6) \\ \hline m\angle A = 46^\circ \end{array}$$

Find the measure of each angle indicated.

41)

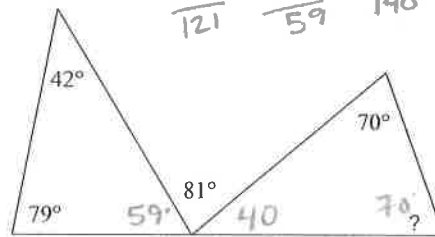


$$\begin{array}{r} 25 \quad 180 \\ +35 \quad -60 \\ \hline 60 \quad 120 \end{array}$$

$$\begin{array}{r} 33 \quad 180 \\ +120 \quad -153 \\ \hline 153 \quad 27 \end{array}$$

$\angle = 27^\circ$

42)



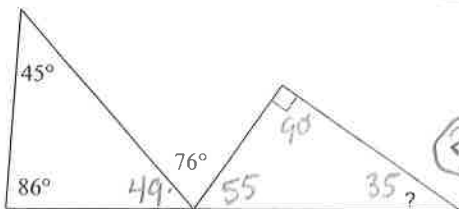
$$\begin{array}{r} 42 \quad 180 \\ +79 \quad -121 \\ \hline 121 \quad 59 \end{array}$$

$$\begin{array}{r} 59 \quad 180 \\ +81 \quad -140 \\ \hline 140 \quad 40 \end{array}$$

$$\begin{array}{r} 40 \quad 180 \\ +70 \quad -110 \\ \hline 110 \quad 70 \end{array}$$

$\angle = 70^\circ$

43)



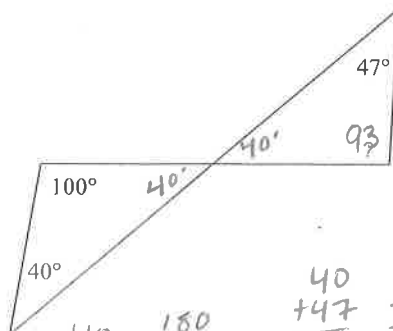
$\angle = 35^\circ$

$$\begin{array}{r} 45 \quad 180 \\ +86 \quad -131 \\ \hline 131 \quad 49 \end{array}$$

$$\begin{array}{r} 49 \quad 180 \\ +76 \quad -125 \\ \hline 125 \quad 55 \end{array}$$

$$\begin{array}{r} 55 \quad 180 \\ +55 \quad -145 \\ \hline 145 \quad 35 \end{array}$$

44)



$\angle = 93$

$$\begin{array}{r} 40 \quad 180 \\ +100 \quad -140 \\ \hline 140 \quad 40 \end{array}$$

$$\begin{array}{r} 40 \quad 180 \\ +47 \quad -87 \\ \hline 87 \quad 93 \end{array}$$

45)

$$\begin{array}{r} 35 \\ + 85 \\ \hline 120 \end{array}$$

$$\begin{array}{r} 180 \\ - 120 \\ \hline 60 \end{array}$$

$$\begin{array}{r} 60 \\ + 89 \\ \hline 149 \end{array}$$

$$\begin{array}{r} 180 \\ - 149 \\ \hline 31 \end{array}$$

$$\begin{array}{r} 31 \\ + 77 \\ \hline 108 \end{array}$$

$$\begin{array}{r} 180 \\ - 108 \\ \hline 72 \end{array}$$

$\angle = 72^\circ$

46)

$$\begin{array}{r} 75 \\ + 65 \\ \hline 140 \end{array}$$

$$\begin{array}{r} 180 \\ - 140 \\ \hline 40 \end{array}$$

$$\begin{array}{r} 90 \\ - 40 \\ \hline 50 \end{array}$$

$$\begin{array}{r} 50 \\ + 20 \\ \hline 70 \end{array}$$

$$\begin{array}{r} 180 \\ - 70 \\ \hline 110 \end{array}$$

$\angle = 110^\circ$

47)

$$\begin{array}{r} 24 \\ + 108 \\ \hline 132 \end{array}$$

$$\begin{array}{r} 180 \\ - 132 \\ \hline 48 \end{array}$$

$$\begin{array}{r} 48 \\ + 49 \\ \hline 97 \end{array}$$

$$\begin{array}{r} 180 \\ - 97 \\ \hline 83 \end{array}$$

$\angle = 83^\circ$

48)

$$\begin{array}{r} 70 \\ + 25 \\ \hline 95 \end{array}$$

$$\begin{array}{r} 180 \\ - 95 \\ \hline 85 \end{array}$$

$$\begin{array}{r} 85 \\ + 55 \\ \hline 140 \end{array}$$

$$\begin{array}{r} 180 \\ - 140 \\ \hline 40 \end{array}$$

$$\begin{array}{r} 40 \\ + 75 \\ \hline 115 \end{array}$$

$$\begin{array}{r} 180 \\ - 115 \\ \hline 65 \end{array}$$

$\angle = 65^\circ$

49)

$$\begin{array}{r} 180 \\ - 151 \\ \hline 29 \end{array}$$

$$\begin{array}{r} 29 \\ + 24 \\ \hline 53 \end{array}$$

$$\begin{array}{r} 180 \\ - 53 \\ \hline 127 \end{array}$$

$\angle = 151^\circ$

50) 
$$\begin{array}{r} 180 \\ -141 \\ \hline 39 \end{array}$$
 
$$\begin{array}{r} 108 \\ +39 \\ \hline 147 \end{array}$$
 
$$\begin{array}{r} 180 \\ -147 \\ \hline 33 \end{array}$$
 
$$\begin{array}{r} 33 \\ +74 \\ \hline 107 \end{array}$$
 
$$\begin{array}{r} 180 \\ -107 \\ \hline 73 \end{array}$$
 
$$\begin{array}{r} 180 \\ -125 \\ \hline 55 \end{array}$$

$$\begin{array}{r} 55 \\ +73 \\ \hline 128 \end{array}$$
 
$$\begin{array}{r} 180 \\ -128 \\ \hline 52 \end{array}$$

51) 
$$\begin{array}{r} 180 \\ -155 \\ \hline 25 \end{array}$$
 
$$\begin{array}{r} 25 \\ +85 \\ \hline 110 \end{array}$$
 
$$\begin{array}{r} 180 \\ -110 \\ \hline 70 \end{array}$$
 
$$\begin{array}{r} 70 \\ +61 \\ \hline 131 \end{array}$$
 
$$\begin{array}{r} 180 \\ -131 \\ \hline 49 \end{array}$$
 
$$\begin{array}{r} 49 \\ +49 \\ \hline 98 \end{array}$$
 
$$\begin{array}{r} 180 \\ -142 \\ \hline 38 \end{array}$$

$$\begin{array}{r} 180 \\ -142 \\ \hline 38 \end{array}$$

52) 
$$\begin{array}{c} 70^\circ \\ ? \end{array}$$
 
$$\text{70}^\circ$$

53) 
$$\begin{array}{c} ? \\ 50^\circ \end{array}$$
 
$$\begin{array}{r} 180 \\ -50 \\ \hline 130 \end{array}$$

54) 
$$\begin{array}{c} 66^\circ \\ ? \end{array}$$
 
$$\text{66}^\circ$$

55) 
$$\begin{array}{c} ? \\ 46^\circ \end{array}$$
 
$$\text{46}^\circ$$

56) 
$$\begin{array}{c} ? \\ 134^\circ \end{array}$$
 
$$\text{134}^\circ$$

57) 
$$\begin{array}{c} ? \\ 46^\circ \end{array}$$
 
$$\text{46}^\circ$$

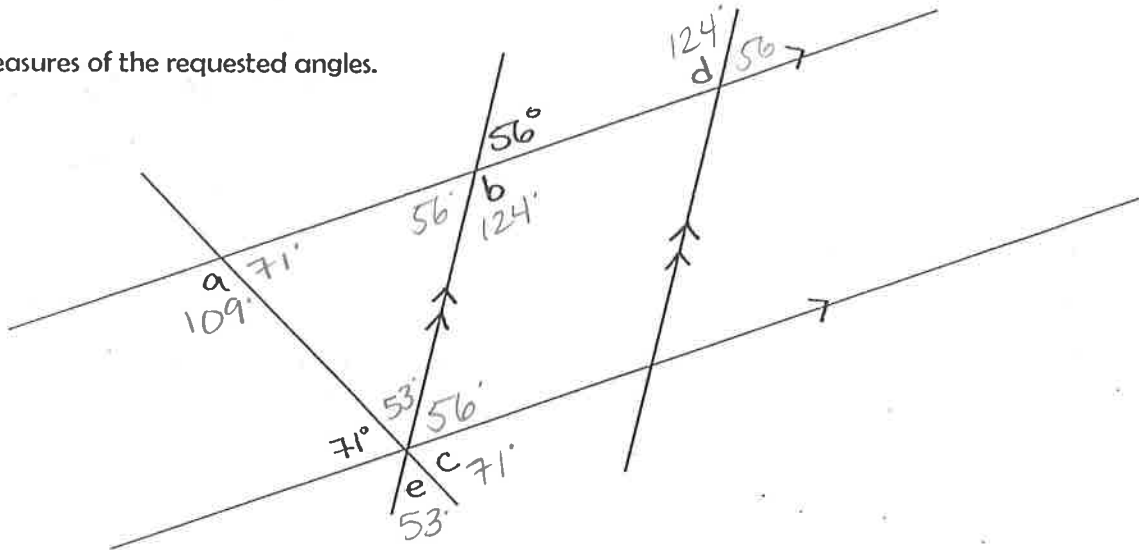
State if the three numbers can be the measures of the sides of a triangle.

- 58) 8, 3,  $\text{8}$   $8+3=11$  Yes      59) 8,  $\text{15}$ , 7  $8+7=15$  No  
 60)  $\text{24}$ , 12, 9  $9+12=21$  No      61) 10,  $\text{19}$ , 9  $9+10=19$  No

Two sides of a triangle have the following measures. Find the range of possible measures for the third side.

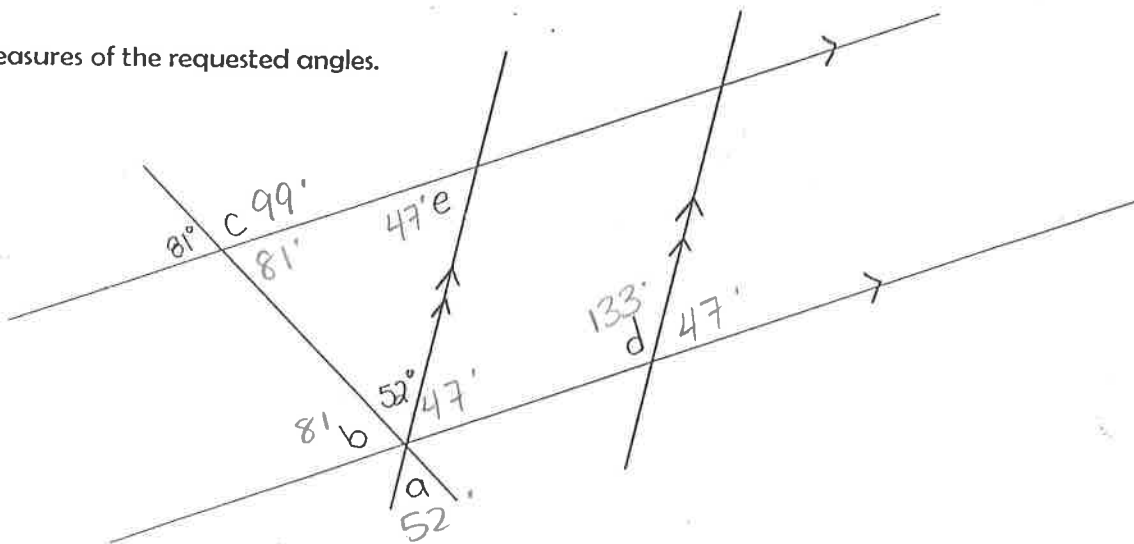
- 62) 10, 8  $2 < x < 18$       63) 11, 12  $1 < x < 23$   
 64) 9, 7  $2 < x < 16$       65) 6, 6  $0 < x < 12$

Find the measures of the requested angles.



- a. 109°    b. 124°    c. 71°    d. 124°    e. 53°

Find the measures of the requested angles.



- a. 52°    b. 81°    c. 99°    d. 133°    e. 47°